## Solution to Ex. 7.17

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Eq. (7.119) on the book is

$$u^{+} = \frac{1}{\kappa} \ln \left( \frac{y}{s} \right) + B_2 \tag{1}$$

we have to associate friction factor f with  $u^+$ , here Eq. (7.106) and Eq. (7.107) come in handy. Considering Eq. (7.104),  $(7.107) \ominus (7.106)$  equals

$$\frac{\langle U \rangle}{u_{\tau}} - \frac{\bar{U}}{u_{\tau}} = u^{+} - \sqrt{\frac{8}{f}} = \frac{3}{2\kappa} + \frac{1}{\kappa} \ln\left(\frac{y}{R}\right)$$
 (2)

substitute  $u^+$  by Eq. (1) and rearrange, we get

$$\sqrt{\frac{8}{f}} = \frac{1}{\kappa} \left( \ln \left( \frac{y}{s} \right) - \ln \left( \frac{y}{R} \right) \right) - \frac{3}{2\kappa} + B_2 \tag{3}$$

the rest of the work is easy.